

Argonne National Laboratory

CRYSTALLOGRAPHIC D-SPACE COMPUTER PROGRAM

by

M. H. Mueller, E. F. H. Meyer,
and S. H. Simonsen

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ABSTRACT

D-Space is a computer program which generates indices $(hk\ell)$, tests for space-group extinctions, and calculates "d," $1/d^2$, $\sin \theta$, $\sin^2 \theta$, $\sin \theta/\lambda$, $\sin^2 \theta/\lambda^2$, θ , and 2θ for any crystal system and space group, requiring only the unit cell constants as data input. Optional calculations are (1) the single-crystal angle settings, phi and chi, and (2) various Lorentz and Lorentz-polarization corrections.

INTRODUCTION

A need for a general, crystallographic computer program for calculating interplanar spacings and several basic trigonometric functions essential in diffraction studies exists. Such a program should be very useful for both powder and single-crystal studies involving neutron and/or X-ray diffraction. Because this program started as a joint effort between individuals at Argonne National Laboratory and The University of Texas, it has currently been used on the CDC-1604 and IBM-704 computers. It has been made available to the computer committee of the American Crystallographic Association for listing.

DISCUSSION

The program, which has been written in Fortran, requires only the unit cell constants as input data, with some choice of output with regard to extinctions and various functions.

Indices are incremented in the order of h , then k , then ℓ . The extinction tests are applied, $\sin \theta$ is computed and tested that its value be < 1 , and the output data are calculated and printed before returning to the main program for the next set of indices. Extinctions are ordered in the format found in Buerger.(1)

After the positive indices have been generated, negative indices are formed. For the triclinic case, all sign permutations are performed; for

the monoclinic case, only h and \bar{h} are computed. Redundant indices in the cubic, hexagonal, and tetragonal cases can be omitted.

Interplanar spacings and related quantities are computed by means of the general quadratic equation

$$Q = 1/d^2 = (ha^*)^2 + (kb^*)^2 + (lc^*)^2$$

$$+ 2(klb^*c^*\cos\alpha^* + hla^*c^*\cos\beta^* + hka^*b^*\cos\gamma^*) .$$

The reciprocal lattice parameters are computed in the usual way:

$$a^* = (bc \sin \alpha)/V ; b^* = (ac \sin \beta)/V ; c^* = (ab \sin \gamma)/V$$

$$V = abc(1 + 2 \cos \alpha \cos \beta \cos \gamma - \cos^2 \alpha - \cos^2 \beta - \cos^2 \gamma)^{1/2}$$

$$\cos \alpha^* = (\cos \beta \cos \gamma - \cos \alpha) / (\sin \beta \sin \gamma)$$

$$\cos \beta^* = (\cos \gamma \cos \alpha - \cos \beta) / (\sin \alpha \sin \gamma)$$

$$\cos \gamma^* = (\cos \alpha \cos \beta - \cos \gamma) / (\sin \alpha \sin \beta) .$$

The single-crystal angle settings phi and chi have the usual meaning as previously described⁽²⁾ and calculated⁽³⁾. The angle phi (ϕ) can be computed for the following 6 different orientations of the crystal:

$$\phi_{c-a} = \tan^{-1} \frac{[V(ck - bl \cos \alpha)]}{bc[bch \sin^2 \alpha + ack(\cos \alpha \cos \beta - \cos \gamma) + abl(\cos \alpha \cos \gamma - \cos \beta)]}$$

$$\phi_{c-b} = \tan^{-1} \frac{[V(ch - al \cos \beta)]}{ac[bch(\cos \alpha \cos \beta - \cos \gamma) + ack \sin^2 \beta + abl(\cos \beta \cos \gamma - \cos \alpha)]}$$

$$\phi_{b-c} = \tan^{-1} \frac{[V(bh - ak \cos \gamma)]}{ab[bch(\cos \alpha \cos \gamma - \cos \beta) + ack(\cos \beta \cos \gamma - \cos \alpha) + abl \sin^2 \gamma]}$$

$$\phi_{b-a} = \tan^{-1} \frac{[V(bl - ck \cos \alpha)]}{bc[bch \sin^2 \alpha + ack(\cos \alpha \cos \beta - \cos \gamma) + abl(\cos \alpha \cos \gamma - \cos \beta)]}$$

$$\phi_{a-b} = \tan^{-1} \frac{[V(al - ch \cos \beta)]}{ca[bch(\cos \alpha \cos \beta - \cos \gamma) + ack \sin^2 \beta + abl(\cos \beta \cos \gamma - \cos \alpha)]}$$

$$\phi_{a-c} = \tan^{-1} \frac{[V(ak - bh \cos \gamma)]}{ba[bch(\cos \alpha \cos \gamma - \cos \beta) + ack(\cos \beta \cos \gamma - \cos \alpha) + abl \sin^2 \gamma]}$$

where the subscripts a, b, and c indicate the relative orientation of the crystal. The first subscript letter indicates the axis of the crystal along

the ϕ axis, and the second subscript letter indicates the reciprocal axis of the crystal in the plane of the χ circle.

The ϕ_{b-a} calculation above would indicate, for example, that the "b" axis was along the ϕ axis, the usual goniometer axis, and that the a^* axis is in the plane of the χ circle, which, with the proper 2θ setting, would be correct for the $h00$ reflections.

Chi can be computed for 3 axial rotations in which the subscript a, b, or c describes the crystal axis - the unique axis - along the ϕ axis of the instrument:

$$\chi_a = \sin^{-1} [(h/a) d_{hkl}]$$

$$\chi_b = \sin^{-1} [(k/b) d_{hkl}]$$

$$\chi_c = \sin^{-1} [(\ell/c) d_{hkl}] .$$

In all of the above it is assumed that $\phi = \chi = 0$ for calculation purposes; however, constant corrections can be added algebraically to phi and chi so that the calculated values correspond to actual goniostat settings.

The following Lorentz or Lorentz-polarization corrections can be computed:

A. Lorentz correction, crystal face, symmetrical reflection:

$$L = 1/\sin 2\theta$$

B. Lorentz correction, Debye-Scherrer lines on cylindrical film:

$$L = \frac{1}{2} \sin^2 \theta \cos \theta$$

C. Lorentz-polarization correction, Debye-Scherrer lines on cylindrical film:

$$L.P. = (1 + \cos^2 2\theta) / \sin^2 \theta \cos \theta$$

D. Lorentz-polarization correction, equi-inclination Weissenberg photographs:

$$L.P. = \frac{(1 + \cos^2 2\theta)}{\sin 2\theta} \frac{\sin \theta}{(\cos^2 \mu - \cos^2 \theta)^{1/2}}$$

Because $\sin \theta$ and $\sin 2\theta$ are computed and stored in the main program, the L. P. correction is calculated by means of the expression

$$L.P. = \frac{(2 - \sin^2 2\theta)}{\sin 2\theta} \frac{\sin \theta}{(\cos^2 \mu + \sin^2 \theta - 1)^{1/2}},$$

where:

$$\cos^2 \mu = [1.0 - (n\lambda/2T)]$$

and

$$T = \text{identity period} .$$

RUNNING TIME

The running time usually varies from 1 to 5 min, depending upon the space group, options chosen, and computer used. The largest problem encountered to date involved over 7000 reflections with phi and chi calculations, and required 40 min on the IBM-704.

FORTRAN NOTATION

<u>Function</u>	<u>Fortran Symbol</u>	<u>Function</u>	<u>Fortran Symbol</u>
$\cos \alpha$	CWA	c^*	CS
$\sin \alpha$	SWA	V (volume)	V
$\cos \beta$	CWB	$Q = 1/d^2$	SUM
$\sin \beta$	SWB	$\sin^2 \theta/\lambda^2$	SQTLS
$\cos \gamma$	CWC	$\sin \theta/\lambda$	SINTL
$\sin \gamma$	SWC	"d"	D
$\cos \alpha^*$	COSAS	θ	THETA
$\cos \beta^*$	COSBS	2θ	TWOTH
$\cos \gamma^*$	COSCS	$\sin 2\theta$	SN2TH
a^*	AS	$\sin \theta$	SINTH
b^*	BS		

All trigonometric functions are calculated by library subroutines.

INPUT CARDS

<u>Card</u>	<u>Columns</u>	<u>Variable</u>	<u>Code Name</u>	<u>Description</u>
1	1 to 72	-	-	Hollerith title card; If program is run under format control, observe limitation for column 1.
2	1 to 10	α	WAD	Lattice constant, decimal point in col. 5
	11 to 20	β	WBD	Lattice constant, decimal point in col. 15
	21 to 30	γ	WCD	Lattice constant, decimal point in col. 25
	31 to 40	a	A	Lattice constant, decimal point in col. 35
	41 to 50	b	B	Lattice constant, decimal point in col. 45
	51 to 60	c	C	Lattice constant, decimal point in col. 55
	61 to 70	λ	XL	Wavelength of radiation, in \AA ; decimal point in col. 64.

Note: All angles should be expressed as degrees and decimal fractions of degrees.

Card

3	Column 1	LA(HKL)
1		omit this and all succeeding tests
2		omit this test, go to next test
3		$h + k + \ell = 2n$, condition for non-extinction
4		$h + k = 2n$
5		$h + \ell = 2n$
6		$k + \ell = 2n$
7		$h + k = 2n$, $h + \ell = 2n$, and $k + \ell = 2n$
8		$- h + k + \ell = 3n$
9		$h + k + \ell = 3n$
	Column 2	LB(OKL)
1		omit this and all succeeding tests
2		omit this test, go to next test
3		$k = 2n$

		$\ell = 2n$
4		
5		$k + \ell = 2n$
6		$k + \ell = 4n$
Column 3	LC(HOL)	
1		omit this and all succeeding tests
2		omit this test, go to next test
3		$h = 2n$
4		$\ell = 2n$
5		$h + \ell = 2n$
6		$h + \ell = 4n$
Column 4	LD(HKO)	
1		omit this and all succeeding tests
2		omit this test, go to next test
3		$h = 2n$
4		$k = 2n$
5		$h + k = 2n$
6		$h + k = 4n$
Column 5	LE(HHL)	
1		omit this and all succeeding tests
2		omit this test, go to next test
3		$\ell = 2n$
4		$h = 2n$
5		$h + \ell = 2n$
6		$2h + \ell = 4n$
Column 6	LF(HOO)	
1		omit this and all succeeding tests
2		omit this test, go to next test
3		$h = 2n$
4		$h = 4n$

Column 7 LG(OKO)

- 1 omit this and all succeeding tests
- 2 omit this test, go to next test
- 3 $k = 2n$
- 4 $k = 4n$

Column 8 LH(OOL)

- 1 omit this and all succeeding tests
- 2 omit this test, go to next test
- 3 $\ell = 2n$
- 4 $\ell = 3n$
- 5 $\ell = 4n$
- 6 $\ell = 6n$

Column 9 LI(HHO)

- 1 omit this test
- 2 $h = 2n$

Column 10 NP(PHI)

- 0 omit this calculation
- 1 calculate ϕ_{c-a}
- 2 calculate ϕ_{c-b}
- 3 calculate ϕ_{b-c}
- 4 calculate ϕ_{b-a}
- 5 calculate ϕ_{a-b}
- 6 calculate ϕ_{a-c}

Column 11 NC(CHI)

- 0 omit this calculation
- 1 calculate χ_c
- 2 calculate χ_b
- 3 calculate χ_a

Column 12 LP(COR)

- 0 omit L or LP calculations
- 1 L for crystal face, symmetrical reflection
- 2 L for Debye-Scherrer Lines on cylindrical film
- 3 LP for Debye-Scherrer lines on cylindrical film
- 4 LP, equi-inclination, a-axis rotation
- 5 LP, equi-inclination, b-axis rotation
- 6 LP, equi-inclination, c-axis rotation

Column 13 NCT

- 0 all values of h , k , and ℓ are computed, with specified extinctions
- 1 criteria $h \geq k \geq \ell$ must be satisfied.
(Cubic case: $h \geq 0$, $k \geq 0$, $\ell \geq 0$)
- 2 criteria $h \geq k$ must be satisfied. (Tetragonal or hexagonal case: $h \geq k$, $h \geq 0$, $k \geq 0$)

Columns 14-20: Should be punched 0 or 1 for sign permutation control.

Column 14

- 0 omit this sign permutation and proceed to next possibility
- 1 calculate $\bar{h}\bar{k}\bar{\ell}$

Column 15

- 0 omit
- 1 calculate $\bar{h}\bar{k}\bar{\ell}$

Column 16

- 0 omit
- 1 calculate $\bar{h}\bar{k}\bar{\ell}$

Column 17

0	omit
1	calculate \overline{hkl}

Column 18

0	omit
1	calculate $\overline{\overline{hkl}}$

Column 19

0	omit
1	calculate $\overline{\overline{\overline{hkl}}}$

Column 20

0	omit
1	calculate $\overline{\overline{\overline{\overline{hkl}}}}$

Columns 21-30: (ADJP) correction to ϕ to be added algebraically to calculated values. Decimal point in col. 25

Columns 31-40: (ADJC) correction to χ to be added algebraically to calculated values. Decimal point in col. 35

Note: In card 3, columns 1-9 must have punches (not 0) in them, otherwise a "computational error" at relative address xxxx will occur. If column 10 is zero, column 11 must also be zero.

In card 3, columns 14-20 are used to control the sign permutation of hkl . If columns 14-20 are punched zero only the hkl case is computed. For example, the following may apply: Monoclinic and hexagonal systems; 14-20, 1000000, orthorhombic, tetragonal and cubic systems and hexagonal powder patterns; 14-20, 0000000.

CARD DECK ARRANGEMENT

IBM-704

D-Space binary program deck
 Card 1. (Title card)
 Card 2. (Cell constants card)

Card 3. (Options card)

Blank card

Blank card

Note 1: When using with the CDC-1604, the deck arrangement may vary according to the compiler system in operation for each computer. The output mode may have to be changed to meet the demands of the individual system, e.g., the WRITE TAPE statement may have to be changed to PRINT.

Note 2: More than one set of computations can be made by using additional data cards 1, 2, and 3 in sequence. These cards should be placed after the initial 3 data cards. The last set of data cards should always be followed by 2 blank cards.

1209/MET 135
704 PROGRAM
Programmer _____ **Date** _____
Meyer and Janousek 6/21/61

GENERAL OPERATING INSTRUCTIONS

USED NOT USED

 DRUM:

 UF SWITCH:
READER: 72 x 72 board

PUNCH: Not used

PRINTER: Not used

SENSE SWITCH SETTINGS: All up

TAPES:
Input: None

Scratch: None

Output - Printed #2

- Punched

To Be Saved

None

Rewound by Program Prior to Calculation None **After** None
Manual EOF Needed
TIME BEFORE OUTPUT:

a few seconds

NORMAL RUNNING TIME: Approx. 30 sec. to 5 min. depending on
RUN NO LONGER THAN: 45 mins. sign permutations and extinction choices.

RUNNING PROCEDURE: (Indicate both regular and restart)

1. READY tape #2.
2. SET underflow switch on.
3. READY binary program deck followed by data cards in reader.
4. CLEAR and LOAD CARDS.
5. HPR 77777₈ in S.R. - problem completed.
6. Write EOF on tape #2, remove, and print off-line.

STOPS (OCTAL): HPR 77777 - End of problem.

HPR 777 - Illegal negative values for NP and/or LP. Press START to read next case.

 HPR 77 - Illegal negative values for NP, LP, and/or NC. Press START to continue without calculating ϕ, χ , or LP.

FORTRAN Error Stops

TEST PROBLEM - ALPHA URANIUM

The test problem selected for this program (MET-135) was that of alpha uranium, which is orthorhombic Space group No. 63, Cmcm, which has the following conditions for the reflections:

$$hkl: h + k = 2n$$

$$h00: (h = 2n)$$

$$0kl: (k = 2n)$$

$$0k0: (k = 2n)$$

$$h0l: l = 2n ; (h = 2n)$$

$$00l: (l = 2n)$$

$$hk0: (h + k = 2n)$$

The lattice constants are indicated in Fig. 1, which is the data sheet used for punching the necessary 3 cards. It can be noted from this sheet that the calculation is for CuK_{α} radiation and that the hkl output has been limited based upon the above reflection conditions. In this test case, one of the options is also being used, namely, the calculation of ϕ and χ based on the b axis of the crystal unique - b axis along the ϕ axis - and the a^* axis of the crystal is in the plane of the χ circle.

The output from an IBM-704 run is shown in Fig. 2. The title and input information, under identifying symbols, are printed on the first few lines, thereby affording a convenient check on input data. The next 2 lines list the unit cell volume, cosines of the reciprocal lattice angles, and the reciprocal lattice parameters. The last portion is a columnar arrangement of the output data in which the following abbreviations are used for column headings:

D	d spacing
$1/DSQ$	$1/d^2$
SINTH	$\sin\theta$
SINTHS	$\sin^2\theta$
SINTL	$\sin\theta/\lambda$
SQTLS	$\sin^2\theta/\lambda^2$
THETA	θ
2THETA	2θ
PHI	ϕ
CHI	χ
LP	Lorentz-polarization correction

704 INPUT DATA

FORM II

COST CODE 1209

FIGURE 1. MET-135 704 DATA SHEET - ALPHA URANIUM TEST PROBLEM

PROGRAM MET 135 PROBLEM Alpha Uranium ORIGINATOR Mueller

DATE 2/28/62

PAGE 1 OF 1

FIGURE 2. MET-135 704 OUTPUT SHEET - ALPHA URANIUM
TEST PROGRAM

1209/MET135 ALPHA URANIUM B AXIS UNIQUE 5/3/62												
ALPHA BETA GAMMA			A B C			LAMBDA						
90.00000 90.00000 90.00000			2.85390 5.86910 4.95540			1.541780						
HKL	OKL	HOL	HKO	HHL	HOO	OKO	OOL	HIO	PHI	CHI	COR	
4	3	4	5	1	3	3	1	4	2	0	0	
V	COSA*	COSB*	COSC*	A*	B*	C*	ADJPHI	ADJCHI				
83-00208	-0.000000	-0.000000	-0.000000	0.350398	0.170384	0.201800	-0.	-0.				
H	K	L	D	1/DSQ	SINTH	SINTHS	SINTL	SQTLS	THETA	2THETA	PHI	CHI
2	0	0	1.42695	0.49111	0.50420	0.29186	0.35040	0.12278	32.69972	65.39944	0.	0.
1	1	0	2.56656	0.15181	0.30036	0.09022	0.19481	0.03795	17.47920	34.95840	-0.00001	25.93174
3	1	0	0.93904	1.13404	0.82093	0.67393	0.53246	0.28351	55.17801	110.35601	-0.00000	9.20679
0	2	0	2.92455	0.11612	0.26269	0.06901	0.17038	0.02903	15.23000	30.46001	45.00001	90.00000
2	2	0	1.28328	0.60724	0.60072	0.36086	0.38963	0.15181	36.92124	73.84284	-0.00001	25.93174
1	3	0	1.61363	0.38405	0.47774	0.22823	0.30986	0.09601	28.53771	57.07541	-0.00002	55.56913
3	3	0	0.85552	1.36628	0.90108	0.81108	0.58844	0.34157	64.30022	128.40044	-0.00001	25.93174
0	4	0	1.46728	0.46449	0.52539	0.27603	0.34077	0.11612	31.69493	63.38886	45.00001	90.00000
2	4	0	1.02297	0.95560	0.75538	0.56789	0.48878	0.23890	48.90178	97.80356	-0.00001	44.20177
1	5	0	1.08558	0.94854	0.71012	0.50527	0.46058	0.21214	45.24443	90.48887	-0.00003	67.64247
0	6	0	0.97818	1.04510	0.77808	0.62108	0.51115	0.26128	52.00676	104.01352	45.00001	90.00000
2	6	0	0.80681	1.55622	0.95547	0.91293	0.61972	0.38405	72.83792	145.67585	-0.00002	55.56913
1	7	0	0.80444	1.54528	0.95829	0.91832	0.62155	0.36362	73.39311	146.78622	-0.00005	73.62785
1	1	1	2.27902	0.19255	0.33826	0.11442	0.21939	0.04813	19.77600	39.54120	29.98489	22.84928
3	1	1	0.92263	1.17476	0.83554	0.69813	0.54193	0.29369	56.67200	113.34418	10.86700	9.04444
0	2	1	2.52501	0.15685	0.30530	0.09321	0.19802	0.03921	17.77631	35.55261	-89.99998	59.36633
2	2	1	1.24230	0.64796	0.62054	0.38506	0.40248	0.16199	38.35522	76.71048	16.04621	25.04534
1	3	1	1.53433	0.42478	0.50243	0.25243	0.32587	0.10619	30.16072	60.32145	29.95838	51.65378
3	3	1	0.84305	1.40701	0.91441	0.83614	0.59309	0.35175	66.12192	132.24840	-0.00000	25.52629
0	4	1	1.40690	0.50521	0.54794	0.30023	0.35539	0.12630	33.22553	66.45110	-89.99998	73.50620
2	4	1	1.00184	0.99633	0.76947	0.59209	0.49908	0.24909	50.30662	100.61323	16.06470	43.06208
1	5	1	1.06043	0.88997	0.72696	0.52847	0.47151	0.22232	46.63191	93.26381	29.98388	64.60922
0	6	1	0.95967	1.05083	0.80329	0.64528	0.52102	0.27146	53.44551	106.89102	-89.99993	78.83535
2	6	1	0.79653	1.57694	0.96806	0.93713	0.62788	0.39424	75.47886	150.95773	16.04024	54.49742
0	0	2	2.47770	0.16229	0.31113	0.09680	0.20180	0.04072	18.12742	36.25484	-90.00000	1.217197
2	0	2	1.23654	0.65401	0.62324	0.38866	0.40435	0.16350	38.56663	77.13325	29.93839	0.
1	1	2	1.78258	0.31470	0.43246	0.18702	0.28049	0.07868	56.26235	51.24710	49.03614	17.68140
3	1	2	0.87810	1.29693	0.87791	0.77073	0.56941	0.32423	61.39145	122.78291	21.00404	8.60452
0	2	2	1.49315	0.27902	0.40720	0.16581	0.26411	0.06975	24.02900	48.05801	-89.99999	40.17509
2	2	2	1.13951	0.77013	0.67651	0.45675	0.43879	0.19253	42.57150	85.14307	29.93839	22.81928
1	3	2	1.35216	0.56495	0.57012	0.32504	0.36978	0.13674	34.75850	69.51699	49.03614	43.72181
3	3	2	0.80867	1.52918	0.95328	0.90875	0.61830	0.38229	72.47178	144.83317	21.00403	24.41564
0	4	2	1.26251	0.62738	0.61060	0.37284	0.39604	0.15685	37.65531	75.26625	-89.99998	59.36633
2	4	2	0.94555	1.11850	0.81529	0.66449	0.52880	0.27962	54.18156	109.23129	29.93838	40.12243
1	5	2	0.99443	1.01144	0.77529	0.60107	0.50285	0.25286	50.50309	101.61691	49.03614	57.89643
0	6	2	0.90984	1.20800	0.84728	0.71788	0.54954	0.30200	57.91671	115.83342	-89.99997	68.45617
1	1	3	1.38900	0.51832	0.55500	0.30802	0.35997	0.12958	35.71052	67.42104	59.93832	13.68967
3	1	3	0.81635	1.50055	0.94432	0.89173	0.61248	0.37514	70.78941	141.57883	29.93838	7.99534
0	2	3	1.43934	0.48263	0.53555	0.26681	0.34736	0.12066	32.38126	64.76252	-89.99999	29.37431
2	2	3	1.01339	0.97375	0.76070	0.57867	0.49339	0.24344	49.52623	99.05246	40.82295	20.20201
1	3	3	1.15427	0.75056	0.66736	0.44664	0.45318	0.18764	41.90220	83.80404	59.93833	36.15740
0	4	3	1.09698	0.83100	0.70274	0.49394	0.45580	0.20775	44.67072	89.29040	-89.99998	48.38570
2	4	3	0.86969	1.32211	0.88639	0.78759	0.57492	0.33053	62.42356	124.84713	40.82295	36.35071
1	5	3	0.90720	1.21505	0.84795	0.72207	0.55115	0.30376	58.16429	116.36858	59.93833	50.61140
0	6	3	0.84167	1.11611	0.91590	0.83886	0.59406	0.35290	66.33453	132.66905	-89.99998	59.36633
0	0	4	1.23885	0.65157	0.62226	0.39721	0.40360	0.16289	38.48155	76.96311	-90.00000	0.
2	0	4	0.93548	1.14269	0.82405	0.67907	0.53448	0.28567	55.49275	110.98550	49.03614	0.
1	1	4	1.11568	0.80338	0.69096	0.47743	0.44816	0.20065	43.70620	87.41239	66.53483	10.95825
0	2	4	1.14132	0.76769	0.67544	0.45622	0.43809	0.19192	42.48832	84.97665	-90.00000	22.88754
2	2	4	0.89129	1.25881	0.86491	0.74807	0.56098	0.31470	59.87274	119.74548	49.03614	17.68140
1	3	4	0.98265	1.03563	0.78450	0.61504	0.50883	0.25891	51.67463	103.34927	66.53483	30.15114
0	4	4	0.94658	1.11606	0.81440	0.66324	0.52822	0.27902	54.52789	109.05577	-89.99999	40.17509
2	4	4	0.76880	1.60718	0.97729	0.95510	0.63587	0.40179	77.76635	155.55271	49.03614	32.52020
1	5	4	0.81646	1.50012	0.94918	0.89148	0.61204	0.37503	76.76888	112.53176	66.53484	44.07204
1	1	5	0.92454	1.16989	0.83581	0.69523	0.54081	0.29274	56.49172	112.96345	70.84933	9.06340
2	2	5	0.93898	1.13420	0.82099	0.67402	0.53250	0.28535	55.18805	110.36811	-90.00000	18.66127
1	3	5	0.84451	1.40214	0.91282	0.83325	0.59206	0.35053	65.89869	131.79737	70.81934	15.50331
0	4	5	0.82128	1.48257	0.93864	0.88105	0.60880	0.37064	69.82485	139.64970	-89.99999	25.57378
0	0	6	0.82590	1.46604	0.93339	0.87122	0.60504	0.36651	68.97020	137.94040	-90.00000	0.
1	1	6	0.78620	1.61785	0.98053	0.96144	0.63597	0.40446	78.67538	157.35076	73.85993	7.69822
0	2	6	0.79501	1.58216	0.96966	0.94023	0.62892	0.39554	75.68492	151.16849	-90.00000	15.71783

SOURCE DECK LISTING

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C      1209/MET135  D SPACE
      DIMENSION FS(3),INDX(7)          4
      COMMON SINTH,XL,LA,LB,LC,LD,LE,LF,LG,LH,LI,NP,       6
      INC,V,A,B,C,BCMA,CAMB,ABMC,CWA,CWB,CWC,SWA,SWB,SWC,LP,NCT,ALPHAP,   8
      2ND,MPP,MPC,ADJP,ADJC          10
      10 FORMAT(6F10.5,F10.6)          12
101 FORMAT( 93HO H K L D           1/DSQ      SINTH      SINTHS  14
      1 SINTL   SQTLS   THETA    2THETA )          16
107 FORMAT(94H          V          COSA*      COSB*      COSG*  18
      X          A*          B*          C*)          20
108 FORMAT (F16.5,6F13.6//)          22
109 FORMAT(106H     ALPHA      BETA      GAMMA      A          B  24
      X          C          LAMBDA          )          26
110 FORMAT (6F10.5, F10.6 //)          28
111 FORMAT(109HO H K L D           1/DSQ      SINTH      SINTHS  30
      1 SINTL   SQTLS   THETA    2THETA   PHI      CHI      )          32
123 FORMAT(22H01209/MET135  D SPACE)          36
710 FORMAT(112H  HKL OKL HOL HKO HOO OKO OOL HHO PHI CHI COR NCT -36
      1KL H-L --L HK- -K H- --- ADJPHI      ADJCHI      )          38
781 FORMAT(100HO H K L D           1/DSQ      SINTH      SINTHS  40
      1 SINTL   SQTLS   THETA    2THETA   L-LP      )          42
1231 FORMAT (72H          )          44
      1          )          46
1998 FORMAT(20(3X,1I1),6X,F10.5,5X,F10.5 //)          48
1999 FORMAT (20I1,2F10.5)          50
1233 READ 1231          52
      WRITE OUTPUT TAPE 2,123
777 READ 10, WAD, WBD,WCD,A,B,C,XL          56
      WRITE OUTPUT TAPE 2,1231
      IF (A) 778,18,778          60
778 READ 1999, LA,LB,LC,LD,LE,LF,LG,LH,LI,NP,NC,LP,NCT,(INDX(NA),NA= 62
      11,7),ADJP,ADJC          63
      WRITE OUTPUT TAPE 2,109
      WRITE OUTPUT TAPE 2,110,WAD,WBD,WCD,A,B,C,XL          66
      WRITE OUTPUT TAPE 2,710
      WRITE OUTPUT TAPE 2,1998,LA,LB,LC,LD,LE,LF,LG,LH,LI,NP,NC,LP,NCT, 70
1(INDX(NA),NA=1,7),ADJP,ADJC          71
      WA = WAD/57.2957895          72
      WB = WBD/57.2957895          74
      WC = WCD/57.2957895          76
      CWA = COSF(WA)          COSA
      CWB = COSF(WB)          COSB
      CWC = COSF(WC)          COSB
      SWA = SINF(WA)          SINA
      SWB = SINF(WB)          SINB
      SWC = SINF(WC)          SINB
      BCMA=CWB*CWC-CWA          90
      CAMB=CWC*CWA-CWB          92
      ABMC=CWA*CWB-CWC          94
      COSAS=BCMA/(SWB*SWC)          96
      COSBS=CAMB/(SWC*SWA)          98
      COSCS=ABMC/(SWA*SWB)          100
      NA=0          109
      V = A*B*C*SQRTF(1.0+2.0*CWA*CWB*CWC-CWA*CWA-CWB*CWB-CWC*CWC)          VOLUM

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AS = B*C*SWA/V	A*
BS = A*C*SWB/V	B*
CS = A*B*SWC/V	C*
WRITE OUTPUT TAPE 2,107	
WRITE OUTPUT TAPE 2,108,V,COSAS,COSBS,COSCS,AS,BS,CS	
761 IF(NP) 82,762,779	114
762 IF(LP) 82,765,782	116
779 WRITE OUTPUT TAPE 2,111	
780 GO TO 783	120
785 WRITE OUTPUT TAPE 2,101	
786 GO TO 783	124
782 WRITE OUTPUT TAPE 2,781	
783 FS (1) = 1.	128
FS (2) = 1.	130
FS (3) = 1.	132
21 FH=1.0	134
FK=0.0	136
FL=0.0	138
3 CALL HKL (FH,FK,FL,AS,BS,CS,COSAS,COSBS,COSCS,FS)	140
IF (SINTH - 1.0) 2,4,4	142
2 FH = FH+ 1.0	144
GO TO 3	146
4 FK = FK + 1.0	148
CALL HKL (FH,FK,FL,AS,BS,CS,COSAS,COSBS,COSCS,FS)	150
IF (SINTH - 1.0) 5,6,6	152
5 FH = 0.0	154
GO TO 3	156
6 FH = 0.0	158
CALL HKL (FH,FK,FL,AS,BS,CS,COSAS,COSBS,COSCS,FS)	160
IF (SINTH - 1.0) 2,8,8	162
8 FH = 0.0	164
FK = 0.0	166
FL = FL + 1.0	168
CALL HKL (FH,FK,FL,AS,BS,CS,COSAS,COSBS,COSCS,FS)	170
IF (SINTH - 1.0) 2,9,9	172
9 FH = FH + 1.0	174
CALL HKL(FH,FK,FL,AS,BS,CS,COSAS,COSBS,COSCS,FS)	176
IF (SINTH - 1.0) 2,20,20	178
20 FH = 0.0	180
FK = FK + 1.0	182
CALL HKL(FH,FK,FL,AS,BS,CS,COSAS,COSBS,COSCS,FS)	184
IF (SINTH - 1.0) 2,16,16	186
16 NA=NA+1	188
GO TO (31,32,33,34,35,36,37,15),NA	
31 IF(INDX(1)) 12,16,12	
12 FS(1)=-1.0	
FS(2)=1.0	
FS(3)=1.0	
GO TO 21	
32 IF(INDX(2)) 13,16,13	
13 FS(1)=1.0	
FS(2)=-1.0	
FS(3)=1.0	
GO TO 21	

```
33 IF(INDX(3)) 14,16,14  
14 FS(1)=-1.0  
   FS(2)=-1.0  
   FS(3)=1.0  
   GO TO 21  
34 IF(INDX(4)) 17,16,17  
17 FS(1)=1.0  
   FS(2)=1.0  
   FS(3)=-1.0  
   GO TO 21  
35 IF(INDX(5)) 19,16,19  
19 FS(1)=-1.0  
   FS(2)=1.0  
   FS(3)=-1.0  
   GO TO 21  
36 IF(INDX(6)) 22,16,22  
22 FS(1)=1.0  
   FS(2)=-1.0  
   FS(3)=-1.0  
   GO TO 21  
37 IF (INDX(7)) 23,16,23  
23 FS(1)=-1.0  
   FS(2)=-1.0  
   FS(3)=-1.0  
   GO TO 21  
82 PAUSE 777  
15 GO TO 1233  
18 STOP 77777  
END (0,1,0,0,1)
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220

222

C 1209/MET135 SUBROUTINE HKL 226
 SUBROUTINE HKL (FH,FK,FL,AS,BS,CS,COSAS,COSBS,COSCS,FS) 228
 DIMENSION FS(3) 230
 COMMON SINTH,XL,LA,LB,LC,LD,LE,LF,LG,LH,LI,NP, 232
 INC,V,A,B,C,BCMA,CAMB,ABMC,CWA,CWB,CWC,SWA,SWB,SWC,LP,NCT,ALPHAP, 234
 2ND,MPP,MPC,ADJP,ADJC 236
 1711 FORMAT(3I4,8F10.5) 238
 711 FORMAT(3I4,9F10.5) 240
 11 FORMAT (3I4, 10F10.5) 242
 FHS = FS(1)*FH 244
 FKS = FS(2)*FK 246
 FLS = FS(3)*FL 248
 SUM = (FHS*AS)**2 + (FKS*BS)**2 + (FLS*CS)**2 + 2.0*(FKS*FLS*BS*CS*COSAS) 250
 1COSAS + FHS*FLS*CS*AS*COSBS + FHS*FKS*AS*BS*COSCS) 252
 SQTLS = SUM/4.0 254
 SINTL = SQRT(FSQTLS) 256
 SINTH = SINTL*XL 258
 CHI = -0.0 258
 C
 IF (SINTH - 1.0) 49,50,50 260
 49 SINTH=SINTH**2 262
 IF (NCT-1) 2000,600,610 NCT
 600 IF(FH-FK)50,605,605 266
 605 IF(FK-FL)50,2000,2000 268
 610 IF(FH-FL)50,2000,2000 270
 2000 GO TO (33,2003,1001,1055,1056,1057,1004,1002,1003),LA 272
 1001 A7 = ABSF(FHS + FKS + FLS) H+K+L=2N
 IF (A7) 121,2003,121 276
 121 IF (A7-2.0)50,2003,123 278
 123 A7 = A7-2.0 280
 GO TO 121 282
 1055 FE=ABSF(FHS+FKS) 284
 751 IF (FE) 752,2003,752 H+K=2N
 752 IF (FE-2.0)50,2003,753 288
 753 FE=FE-2.0 290
 C
 GO TO 752 292
 1056 FI=ABSF(FHS+FLS) 294
 761 IF (FI) 762,2003,762 296
 762 IF (FI-2.0)50,2003,763 H+L=2N 300
 763 FI=FI-2.0 302
 GO TO 762 304
 1057 FO=ABSF(FKS+FLS) 306
 771 IF (FO) 772,2003,772 308
 772 IF (FO-2.0)50,2003,773 310
 773 FO=FO-2.0 312
 GO TO 772 314
 1004 DA=ABSF(FHS+FKS) L+K=2N
 IF (DA) 141,145,141 318
 141 IF (DA-2.0)50,145,142 320
 142 DA=DA-2.0 322
 GO TO 141 324
 145 E=ABSF(FHS+FLS) H+L=2N
 140 IF (E) 146,2003,146 328

146 IF (E-2.0)50,2003,147	330
147 E=E-2.0	332
GO TO 146	334
1002 B7 = ABSF(-FHS+FKS+FLS)	K+L-H=3N
IF (B7) 143,2003,143	338
143 IF (B7) 50,2003,144	340
144 B7 = B7-3.0	342
GO TO 143	344
1003 C7 = ABSF(FHS+FKS+FLS)	H+K+L=3N
IF (C7)131,2003,131	348
131 IF (C7-3.0)50,2003,132	350
132 C7 = C7-3.0	362
GO TO 131	354
2003 IF(FH) 2005,2004,2005	356
2004 GO TO (33,2005,1009,1010,1011,1012),LB	358
1009 P=FK	K=2N
IF (P) 161,2005,161	362
161 IF (P-2.0)50,2005,162	364
162 P=P-2.0	366
GO TO 161	368
1010 QA = FL	L=2N
IF (QA) 163,2005,163	372
163 IF (QA-2.0) 50,2005,164	374
164 QA=QA-2.0	376
GO TO 163	378
1011 R=ABSF(FKS+FLS)	K+L=2N
IF (R) 165, 2005, 165	382
165 IF(R-2.0)50,2005,166	384
166 R=R-2.0	386
GO TO 165	388
1012 S=ABSF(FKS+FLS)	K+L=4N
IF (S) 167,2005,167	392
167 IF(S-4.0)50,2005,168	394
168 S=S-4.0	396
GO TO 167	398
2005 IF(FK) 2007,2006,2007	400
2006 GO TO (33,2007,1027,1026,1024,1025),LC	402
1027 AC=FH	H=2N
IF (AC) 187,2007,187	406
187 IF(AC-2.0)50,2007,188	408
188 AC=AC-2.0	410
GO TO 187	412
1026 AB=FL	L=2N
IF (AB) 185,2007,185	416
185 IF(AB-2.0)50,2007,186	418
186 AB=AB-2.0	420
GO TO 185	422
1024 Z=ABSF(FHS+FLS)	H+L=2N
IF (Z) 181,2007,181	426
181 IF(Z-2.0)50,2007,182	428
182 Z=Z-2.0	430
GO TO 181	432
1025 AA=ABSF(FHS+FLS)	H+L=4N
IF (AA) 183,2007,183	436

		438
183	IF(AA-4.0)50,2007,184	440
184	AA=AA-4.0	442
	GO TO 183	444
2007	IF (FL) 2001,2008,2001	446
2008	GO TO (33,2001,1030,1031,1032,1033),LD	H=2N
1030	AF=FH	450
	IF (AF) 195,2001,195	452
195	IF (AF-2.0)50,2001,196	454
196	AF=AF-2.0	456
	GO TO 195	K=2N
1031	AG=FK	460
	IF (AG) 197,2001,197	462
197	IF (AG-2.0)50,2001,198	464
198	AG=AG-2.0	466
	GO TO 197	H+K=2N
1032	AH=ABSF(FHS+FKS)	470
	IF (AH) 199,2001,199	472
199	IF (AH-2.0)50,2001,200	474
200	AH=AH-2.0	476
	GO TO 199	H+K=4N
1033	AI=ABSF(FHS+FKS)	480
	IF (AI) 201,2001,201	482
201	IF (AI-4.0) 50,2001,202	484
202	AI=AI-4.0	486
	GO TO 201	488
2001	IF (FHS-FKS)1028,2002,1028	490
2002	GO TO (33,1028,1005,1006,1007,1008),LE	L=4N
1005	F = FL	494
	IF (F) 151,1028,151	496
151	IF (F-2.0) 50,1028,152	498
152	F = F - 2.0	500
	GO TO 151	H=2N
1006	G=FH	504
	IF (G) 153,1028,153	506
153	IF (G-2.0) 50,1028,154	508
154	G=G-2.0	510
	GO TO 153	H+L=2N
1007	H=ABSF(FHS+FLS)	514
	IF (H) 155,1028,155	516
155	IF (H-2.0) 50,1028,156	518
156	H=H-2.0	520
	GO TO 155	2H+L=4N
1008	O=ABSF(FHS+FHS+FLS)	524
	IF (O) 157,1028,157	526
157	IF (O-4.0) 50,1028,158	528
158	O = O-4.0	530
	GO TO 157	532
1028	IF (FL) 1013,1029,1013	534
1029	IF (FK) 1013,2009,1013	536
2009	GO TO (33,1013,189,192),LF	H=2N
189	AD = FH	540
	IF (AD) 190,1013,190	542
190	IF (AD-2.0)50,1013,191	544
191	AD=AD-2.0	

GO TO 190	546
192 AE=FH	548
193 IF (AE-4.0)50,1013,194	H=4N
194 AE=AE-4.0	552
GO TO 193	554
1013 IF (FL) 1017,2050,1017	556
2050 IF (FH) 1017,2051,1017	558
2051 GO TO (33,1017,1015,1016), LG	560
1015 T=FK	K=2N
IF (T) 169,1017,169	564
C	566
169 IF (T-2.0)50,1017,170	568
170 T=T-2.0	570
GO TO 169	572
1016 U=FK	K=4N
IF (U) 171,1017,171	576
171 IF (U-4.0)50,1017,172	578
172 U=U-4.0	580
GO TO 171	582
1017 IF (FK) 1034,2055,1034	00L
2055 IF (FH) 1034,1018,1034	586
1018 GO TO (33,1034,1019,1020,1021,1022), LH	588
1019 V=FL	L=2N
IF (V) 173,1034,173	592
173 IF (V-2.0) 50,1034,174	594
174 V=V-2.0	596
GO TO 173	598
1020 W = FL	L=3N
IF (W) 175,1034,175	602
175 IF (W-3.0) 50,1034,176	604
176 W=W-3.0	606
GO TO 175	608
1021 X=FL	L=4N
IF (X) 177,1034,177	612
177 IF (X-4.0) 50,1034,178	614
178 X=X-4.0	616
GO TO 177	618
1022 Y=FL	L=6N
IF (Y) 179,1034,179	622
179 IF (Y-6.0) 50,1034,180	624
180 Y=Y-6.0	626
GO TO 179	628
1034 IF (FH-FK)33,2060,33	HH0
2060 IF (FL) 33,2061,33	H=2N
2061 GO TO (33,1035), LI	634
1035 AJ=FH	636
IF (AJ) 203,33,203	638
203 IF(AJ-2.0)50,33,204	640
204 AJ=AJ-2.0	642
GO TO 203	644
33 D = 1.0/SQRTF(SUM)	646
750 THETA=ASINF(SINTH)	648
TWOTH=THETA*2.0	650
SN2TH = SINF(TWOTH)	652

1965 IF(LP)998,890,1966	654
1966 GO TO (1967,1969,1972,1974,1977,1980), LP	656
1967 SLP = 1.0 / SN2TH	658
1968 GO TO 45	660
1969 SLP=1.0/(SINTHS*2.0*COSF(THETA))	662
1970 GO TO 45	664
1972 SLP=(1.0+COSF(TWOTH)**2)/(SINTHS*COSF(THETA))	666
1973 GO TO 45	668
1974 COSQMU = 1.0 - ((FH*XL)/(2.0*A))**2	670
GO TO 1975	672
1977 COSQMU = 1.0 - ((FK*XL)/(2.0*B))**2	674
GO TO 1975	676
1980 COSQMU = 1.0 - ((FL*XL)/(2.0*C))**2	678
C EQUI INCLINATION LP CORRECTION	680
1975 SLP = (2.0-SN2TH*SN2TH)*SINTH/(SN2TH*SQRTF(COSQMU+SINTHS-1.0))	682
GO TO 45	684
890 IF(NP)998, 45,900	686
900 GO TO (905,910,915,920,925,930),NP	PHI
905 TNPBA=(V*(C*FKS-B*FLS*CWA))/(B*C*(1B*C*FHS*SWA**2+A*C*FKS*ABMC+A*B*FLS*CAMB))	690
PHI=ATANF(TNPBA)*57.2957895	692
909 GO TO 940	694
910 TNPBC=(V*(C*FHS-A*FLS*CWB))/(A*C*(B*C* IFHS*ABMC+A*C*FKS*SWB**2+A*B 2*FLS*BCMA))	696
PHI=ATANF(TNPBC)*57.2957895	700
914 GO TO 940	702
915 TNPCB=(V*(B*FHS-A*FKS*CWC))/(A*B*(B* 1C*FHS*CAMB+A*C*FKS*BCMA+A*B*FLS*SWC**2))	704
PHI=ATANF(TNPCB)*57.2957895	708
919 GO TO 940	710
920 TNPBC=(V*(B*FLS-C*FKS*CWA))/(B*C*(B* 1C*FHS*SWA**2+A*C*FKS*ABMC+A*B*FLS*CAMB))	712
PHI=ATANF(TNPBC)*57.2957895	716
924 GO TO 940	718
925 TNPAE=(V*(A*FLS-C*FHS*CWB))/(A*C*(B* 1*C*FHS*ABMC+A*C*FKS*SWB**2+A*B*FLS*BCMA))	720
PHI=ATANF(TNPAE)*57.2957895	722
929 GO TO 940	726
930 TNPAF=(V*(A*FKS-B*FHS*CWC))/(B*A*(B*C 1*FHS*CAMB+A*C*FKS*BCMA+A*B*FLS*SWC**2))	728
PHI=ATANF(TNPAF)*57.2957895	730
940 PHI = PHI + ADJP	732
949 IF(NC)998,45, 950	734
950 GO TO (955,960,965),NC	CH1
955 SNCC=FLS*D/C	742
IF (ABSF(SNCC)-1.) 22222,22221,22221	744
22222 CHI=ASINF(SNCC)*57.2957895	746
959 GO TO 35	748
960 SNCB=FKS*D/B	750
IF (ABSF(SNCB)-1.) 22223,22221,22221	752
22223 CHI=ASINF(SNCB)*57.2957895	754
964 GO TO 35	756
965 SNCA=FHS*D/A	758
	760

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IF (ABSF(SNCA)-1.) 22224,22221,22221          762
22224 CHI=ASINF(SNCA)*57.2957895             764
      GO TO 35                                  766
C
22221 CHI = 90.                                768
 35 CHI = CHI + ADJC                         770
 45 ISA = FHS                                772
    KSA = FKS                               774
    LSA = FLS                                776
    THETA=THETA*57.2957895                  778
    TWOOTH = THETA*2.0                         780
 970 IF(NP)996,975,996                         782
 975 IF(LP)977,980,977                         784
 980 WRITE OUTPUT TAPE 2,1711,ISA,KSA,LSA,D,SUM,SINTH,SINTHS,SINTL,
    ISQTLS,THETA,TWOOTH                      786
 985 GO TO 50                                  790
 977 WRITE OUTPUT TAPE 2, 711,ISA,KSA,LSA,D,SUM,SINTH,SINTHS,SINTL,
    ISQTLS,THETA,TWOOTH,SLP                  794
 996 WRITE OUTPUT TAPE 2, 11,ISA,KSA,LSA,D,SUM,SINTH,SINTHS,SINTL,
    ISQTLS,THETA,TWOOTH,PHI,CHI              802
 997 GO TO 50                                  804
 998 PAUSE 77                                 806
      GO TO 45
 50 RETURN
END (0,1,0,0,1)                                808

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